

SM3 10.1: Graphing Sine & Cosine

Vocabulary: amplitude, period, midline, phase shift, vertical shift, frequency

Problems:

Identify the amplitude and period for each problem.

1) $f(x) = \sin(4x)$

2) $y = 2 \cos(x)$

3) $g(x) = 4 \sin(3x)$

4) $h(x) = \cos(.5x + 2)$

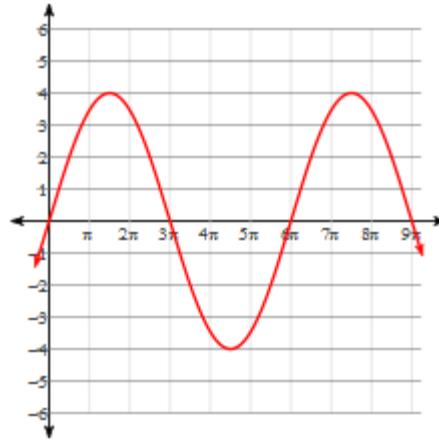
5) $y = 4 + \sin\left(\frac{3}{2}x\right)$

6) $f(x) = -2 + \cos(2x + 6)$

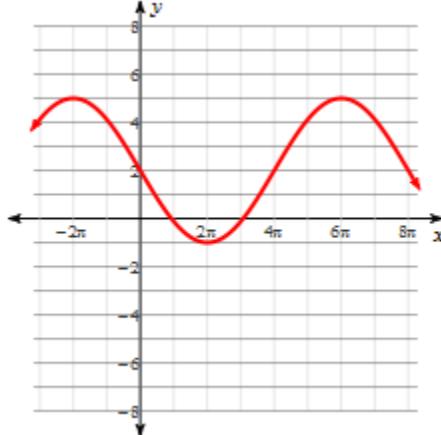
7) $f(x) = \frac{1}{2}\cos(x - 2) + 1$

8) $g(x) = -3 \sin(-x)$

9)



10)



Describe how changes in the given variable change the shape of the curve of $y = \sin x$:

$$y = a \sin(b(x - h)) + k$$

11) $k = 2$

13) $a = 2$

15) $b = 2$

17) $h = -\pi$

12) $k = \frac{1}{3}$

14) $a = \frac{1}{3}$

16) $b = \frac{1}{3}$

18) $h = \frac{\pi}{3}$

Sketch an appropriate coordinate axis and graph two periods of the function.

19)

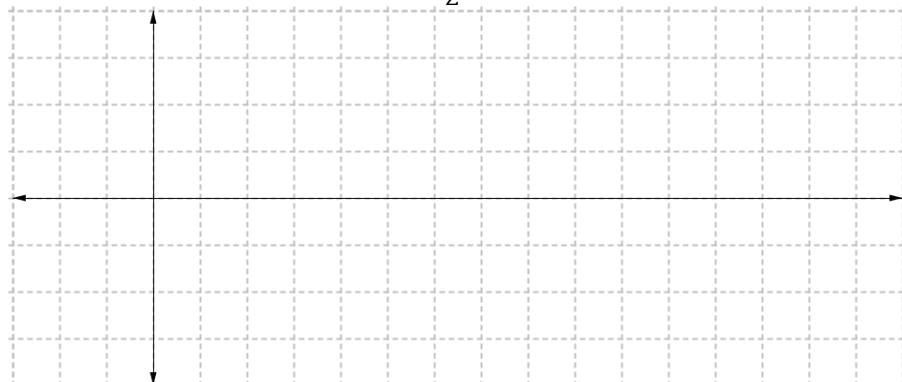
$$y = 3 \sin x$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

20)

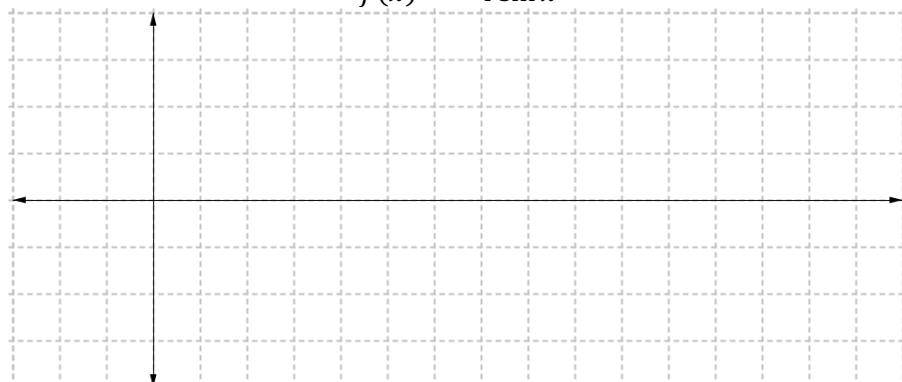
$$y = \frac{1}{2} \cos x$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

21)

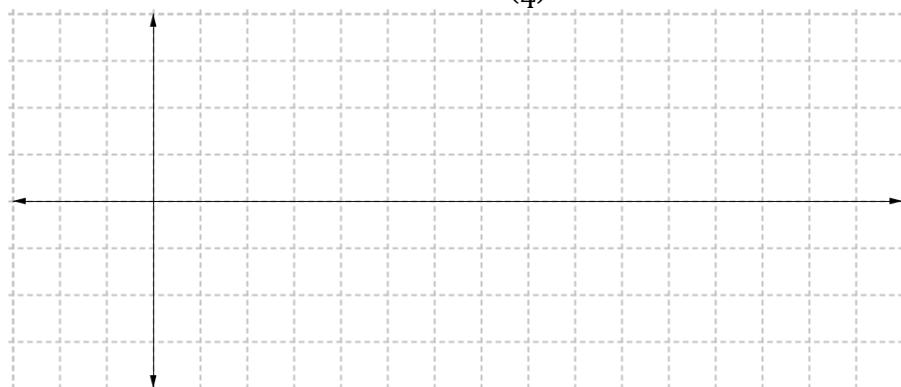
$$f(x) = -4 \sin x$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

22)

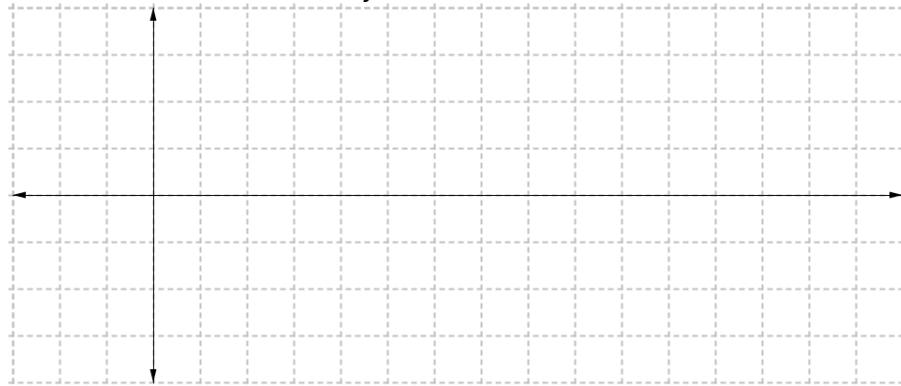
$$g(x) = \sin\left(\frac{x}{4}\right)$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

23)

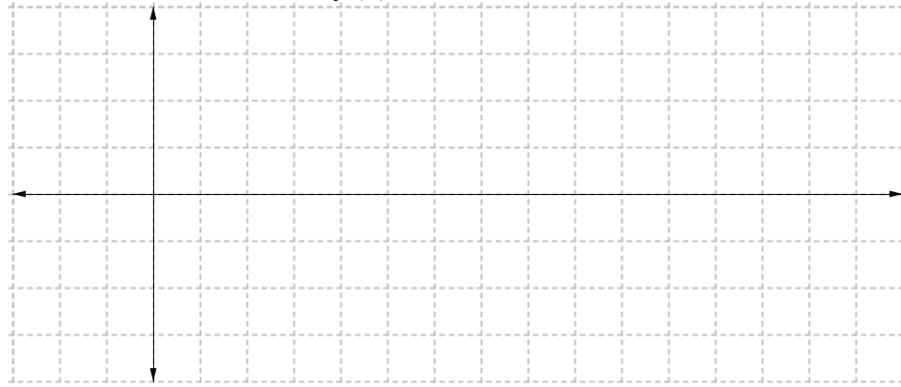
$$y = 1 + 2 \cos x$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

24)

$$f(x) = -2 + 3 \sin x$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

25)

$$h(x) = \sin\left(x - \frac{\pi}{2}\right)$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

26)

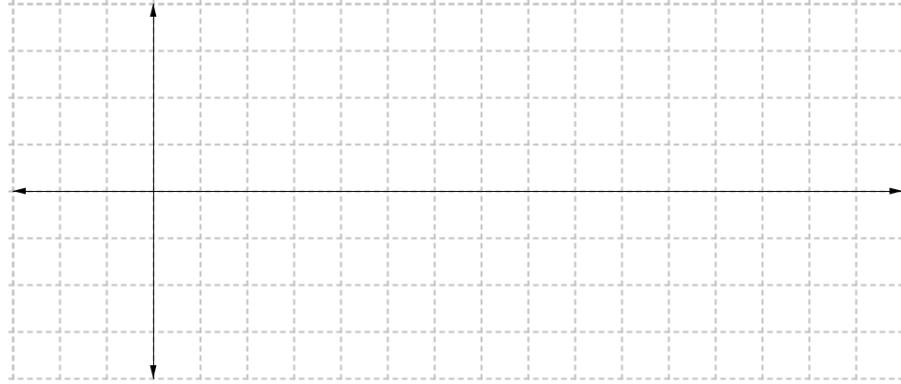
$$y = \cos(x + \pi)$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

27)

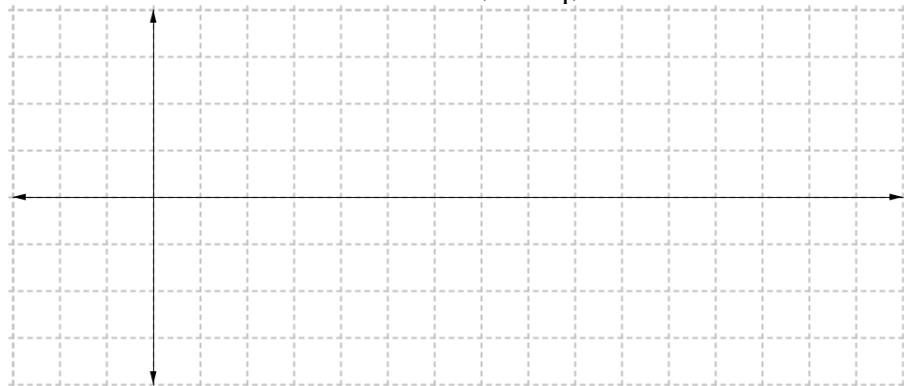
$$g(x) = \sin(2x - \pi)$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

28)

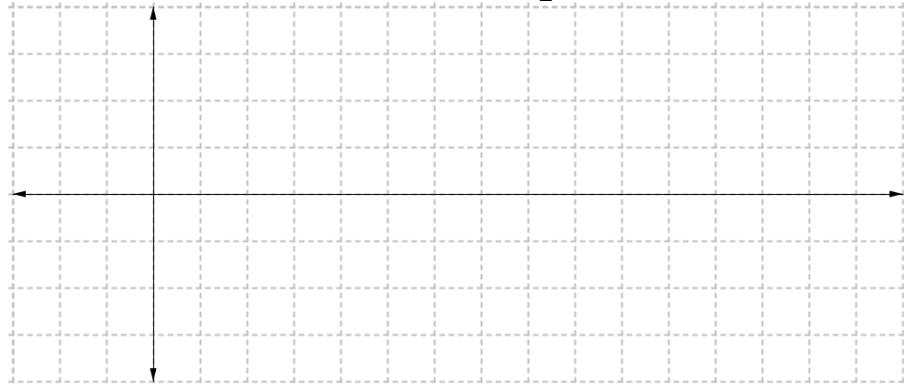
$$f(x) = \cos\left(3x + \frac{\pi}{4}\right)$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

29)

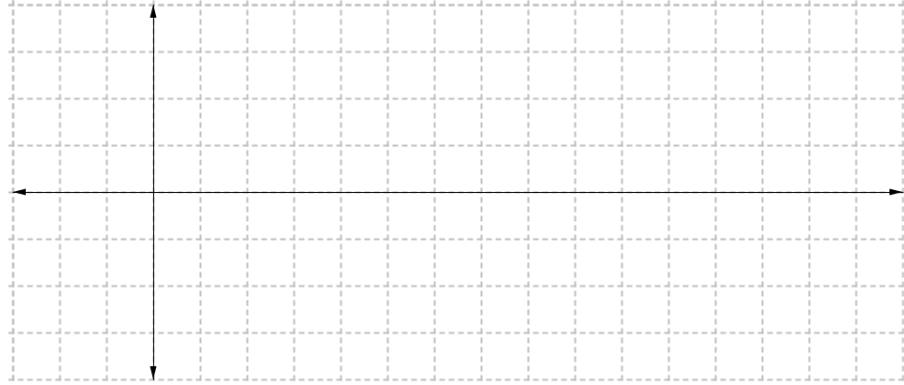
$$f(x) = 3 \sin\left(2x - \frac{\pi}{2}\right) - 2$$



Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

30)

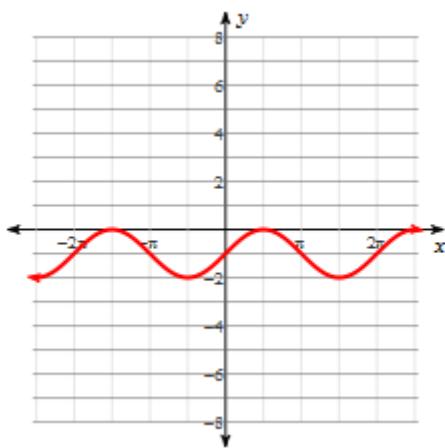
$$y = 1 + 2 \cos\left(3x - \frac{\pi}{2}\right)$$



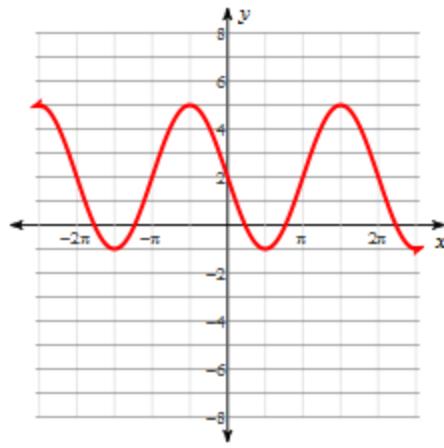
Amp:	
Per:	
P.S.:	
V.S.:	
Scale:	

For 31-32, write the simplest form of a) the sine function and b) the cosine function for the graphs shown below.

31)



32)



- 33) The frequency of a sound wave is 750 cycles per second. If the sound intensity can be modeled by the sine function $S(t) = 0.05 \sin(750t)$, what is the period of the sound wave?
- 34) The voltage in an alternating current circuit can be modeled by the function $V(t) = 175 \sin(110\pi t)$. How many times does the voltage reach a peak positive or negative value in 1 second?
- 35) The alarm in a smoke detector produces a high-pitched sound when smoke is detected. The intensity of the sound can be modeled by the function $I(t) = \cos(3 \cdot 10^4 \cdot \pi \cdot t)$. What are the period and frequency of the sound intensity? The frequency is measured in cycles per second.